

Franklin W. Olin College of Engineering  
ENGR 3310: Transport Phenomena

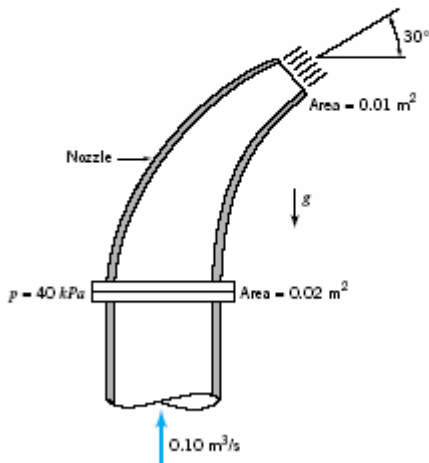
Problem Set 3

Assigned: 9/23/04  
Due: 9/30/04 by 5:00 pm

Fall 2004

Problem 1

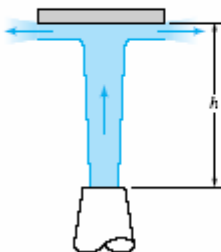
**5.31** A nozzle is attached to a vertical pipe and discharges water into the atmosphere as shown in Fig. P5.31. When the discharge is  $0.1 \text{ m}^3/\text{s}$ , the gage pressure at the flange is  $40 \text{ kPa}$ . Determine the vertical component of the anchoring force required to hold the nozzle in place. The nozzle has a weight of  $200 \text{ N}$ , and the volume of water in the nozzle is  $0.012 \text{ m}^3$ . Is the anchoring force directed upward or downward?



■ FIGURE P5.31

Problem 2

**5.60** A vertical jet of water leaves a nozzle at a speed of  $10 \text{ m/s}$  and a diameter of  $20 \text{ mm}$ . It suspends a plate having a mass of  $1.5 \text{ kg}$  as indicated in Fig. P5.60. What is the vertical distance  $h$ ?



■ FIGURE P5.60

### Problem 3

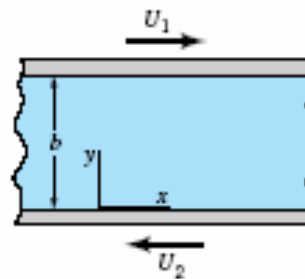
**5.46** The propeller on a swamp boat produces a jet of air having a diameter of 3 ft as illustrated in Fig. P5.46. The ambient air temperature is 80 °F, and the axial velocity of the flow is 85 ft/s relative to the boat. What propulsive forces are produced by the propeller when the boat is stationary and when the boat moves forward with a constant velocity of 20 ft/s?



■ FIGURE P5.46

### Problem 4

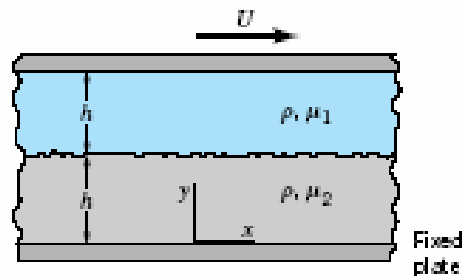
**6.80** An incompressible, viscous fluid is placed between horizontal, infinite, parallel plates as is shown in Fig. P6.80. The two plates move in opposite directions with constant velocities,  $U_1$  and  $U_2$ , as shown. The pressure gradient in the  $x$  direction is zero and the only body force is due to the fluid weight. Use the Navier–Stokes equations to derive an expression for the velocity distribution between the plates. Assume laminar flow.



■ FIGURE P6.80

### Problem 5

**6.81** Two immiscible, incompressible, viscous fluids having the same densities but different viscosities are contained between two infinite, horizontal, parallel plates (Fig. P6.81). The bottom plate is fixed and the upper plate moves with a constant velocity  $U$ . Determine the velocity at the interface. Express your answer in terms of  $U$ ,  $\mu_1$ , and  $\mu_2$ . The motion of the fluid is caused entirely by the movement of the upper plate; that is, there is no pressure gradient in the  $x$  direction. The fluid velocity and shearing stress is continuous across the interface between the two fluids. Assume laminar flow.



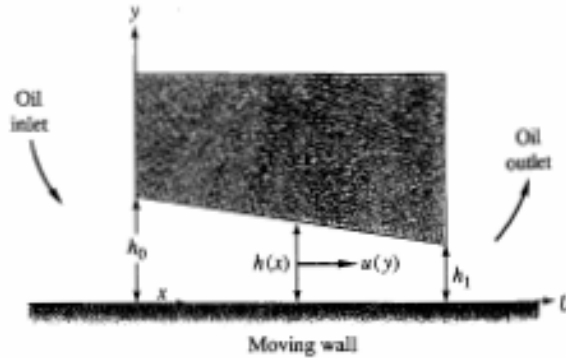
■ FIGURE P6.81

Problem 6 (sorry about the fuzziness – I’ll put a better copy on line by Friday)

**P4.83** The flow pattern in bearing lubrication can be illustrated by Fig. P4.83, where a viscous oil ( $\rho, \mu$ ) is forced into the gap  $h(x)$  between a fixed slipper block and a wall moving at velocity  $U$ . If the gap is thin,  $h \ll L$ , it can be shown that the pressure and velocity distributions are of the form  $p = p(x)$ ,  $u = u(y)$ ,  $v = w = 0$ . Neglecting gravity, reduce the Navier-Stokes equations (4.38) to a single differential equation for  $u(y)$ . What are the proper boundary conditions? Integrate and show that

$$u = \frac{1}{2\mu} \frac{dp}{dx} (y^2 - yh) + U \left( 1 - \frac{y}{h} \right)$$

where  $h = h(x)$  may be an arbitrary, slowly varying gap width. (For further information on lubrication theory, see Ref. 16.)



**P4.83**